

科目：電磁學 適用：電機所系統組

編號：443

考生注意：

1. 依次序作答，只要標明題號，不必抄題。
2. 答案必須寫在答案卷上，否則不予計分。
3. 限用藍、黑色筆作答；試題須隨卷繳回。

本 試 題
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1. A long dielectric cylinder of radius b and dielectric constant ϵ_r is placed along the z -axis in a uniform electric field $\mathbf{E}_0 = \mathbf{a}_x E_0$. Determine the potential distribution $V(r, \phi)$ and electric field intensity $\mathbf{E}(r, \phi)$ both inside and outside the cylinder. (20%)
2. A ferromagnetic sphere of radius b is magnetized uniformly with a magnetization $\mathbf{M} = \mathbf{a}_z M_0$. (a) Determine the equivalent magnetization current density \mathbf{J}_m and surface current density \mathbf{J}_{ms} . (10%) (b) Determine the magnetic flux density at the center of the sphere. (10%)
3. Derive the general wave equations for \mathbf{E} and \mathbf{H} in a non-conducting simple medium where a charge distribution ρ and a current distribution \mathbf{J} exist. Convert the wave equations to Helmholtz's equations for sinusoidal time dependence. (20%)
4. A perpendicular polarized uniform plane wave in air of frequency f is incident obliquely at an angle of incidence θ_i on a plane boundary with a dielectric medium characterized by a complex permittivity $\epsilon_2 = \epsilon_0 - j\epsilon_1$. Let the incident electric field be $\mathbf{E}_i(x, z) = \mathbf{a}_y E_{i0} \exp[-jk_0(x \sin \theta_i - z \cos \theta_i)]$. (a) Find the expressions of the transmitted electric and magnetic field intensity phasors in terms of the given parameters. (14%) (b) Show that the angle of refraction is complex and the \mathbf{H}_t is elliptically polarized. (6%)
5. A small filamentary rectangular loop of dimensions L_x and L_y lies in the xy -plane with its center at the origin and sides parallel to the x - and y -axes. The loop carries a current $i(t) = I_0 \cos \omega t$. Assuming L_x and L_y to be much less than the wavelength, find the instantaneous expressions for the following quantities at a point in the far zone:
 - (a) vector magnetic potential \mathbf{A} (10%), (b) electric field intensity \mathbf{E} (5%),
 - (c) magnetic field intensity \mathbf{H} . (5%)